10 — DELVING INTO DATA

@whisto maths

Collecting, representing and interpreting

What do I need to be able to do?

Bu the end of this unit you should be able to:

- Construct and interpret frequency tables and polygon. two-way tables, line, bar, & pie 1
- Find and interpret averages from a list and
- Construct and interpret time series graphs, stem and leaf diagrams and scatter araphs

Keywords

Population: the whole group that is being studied

Sample: a selection taken from the population that will let you find out information about the larger group Representative: a sample group that accurately represents the population

Random sample: a group completely chosen by change. No predictability to who it will include.

Bias: a built-in error that makes all values wrong by a certain amount

Primary data: data collected from an original source for a purpose.

Secondary data: data taken from an external location. Not collected directly.

Outlier: a value that stands apart from the data set

Frequency tables and polygons

x Weight(g)	Frequency
$40 < x \le 50$	1
$50 < x \le 60$	3
$60 < x \le 70$	5

We do not know from grouped data where each value is placed so have to use an estimate for calculations

MID POINTS Mid-points are used as estimated values for grouped data. The middle of each group

Each point is plotted at them mid point for the group it represents Each point is connected with a straight line. Weight (g)

The data about weiaht starts at 40. So the axis can start at 40

Compare the bars green compared to yellow. The

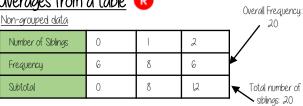
Mid-point				
Start point + End point				
2				

Bar and line charts

size of each bar is the frequency Composite bar charts Overall total easily comparable Dual bar charts Bars are compared side by side. Categories clearly indicated Easier to compare subgroups

Categories clearly indicated

Overages from a table



The data in a list: 0,0,0,0,0,0,1,1,1,1,1,1,1,2,2,2,2,2

Mean: total number of siblings Total frequency

Grouped data

X	Frequency	Mid Point	MP x Freq
Weight(g) $40 < x \le 50$	1	45	45
50 < <i>x</i> ≤ 60	3	65	195
60 < <i>x</i> ≤ 70	5	65	325

Overall Total: 565 Mean: 628g

Overall Frequency: 9

Two way tables

60 people visited the zoo one Saturday morning 26 of them were adults 13 of the adult's favourite animal was an elephant. 24 of the children's favourite animal was an elephant

> Extract information to input to the two-way table

Subgroups each have their own heading

	Odult	Child	Total
Elephant	13	24	37
Other	13	10	23
Total	26	34	60 🗸

Needs subgroup totals

Overall total

Draw and interpret Pie Charts



(Total frequency)

Os 60 goes into 360 — 6 times. Each frequency can be multiplied by 6 to find the degrees (proportion of 360)

There were 60 people asked in this survey

Comparing Pie Charts:

Use a protractor to draw This is 192°

You NEED the overall frequency to make any comparisons

Overages from lists

The Mean

a measure of average to find the central tendency... a typical value that represents the data

24, 8, 4, II, 8,

Find the sum of the data (add the values

55 Divide the overall total by how many pieces of data you have

 $55 \div 5$

Mean = 11

The Mode (The modal value)

This is the number OR the item that occurs the most (it does not have to be numerical)

24, 8, 4, 11, 8,

This can still be easier if it the data is ordered first

Mode = 8

The Median

The value in the center (in the middle) of the data

24, 8, 4, II, 8

Put the data in order

4, 8, 8, 11, 24

Find the value in the middle 4, 8, 8, 11, 24

Median = 8

NOTE: If there is no single middle value find the mean of the two numbers left.

For Grouped Data

The modal group — which group has the highest frequency,

The data in a list: 45, 55, 55, 55, 65, 65, 65, 65, 65

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Stem and leaf

O way to represent data and use to find averages

This stem and leaf diagram shows the age of people in a line at the supermarket.

0 | 7 9 4 5 6 8 8 Key: 1 4 Means 14 years old

2

1 3

Stem and leaf diagrams:

Must include a key to explain what it represents The information in the diagram should be ordered

Back to back stem and leaf diagrams

Girls		Boys	
5	14		
7, 5, 5, 5, 4 8, 4, 2, 1, 0 9, 8, 7, 6, 6, 4, 2, 1, 1, 0, 0	15	3, 8, 9	15 3,
8, 4, 2, 1, 0	16	2, 5, 7, 7, 7, 8, 8, 9	Means 153 cm tall
9, 8, 7, 6, 6, 4, 2, 1, 1, 0, 0	17	0, 2, 3, 6, 6, 7, 7	
	18	0, 1, 4, 5	

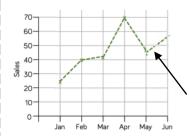
Back to back stem and leaf diagrams

Ollow comparisons of similar groups

Ollow representations of two sets of data

Time-Series

This time-series graph shows the total number of car sales in £ 1000 over time



Look for general trends in the data. Some data shows a clear increase or a clear decrease over time

Readings in-between points are estimates (on the dotted lines). You can use them to make assumptions.

Comparing distributions

Comparisons should include a statement of average and central tendency, as well as a statement about spread and consistency

Mean, mode, median — allows for a comparison about more or less average Range — allows for a comparison about reliability and consistency of data

Draw and interpret a scatter graph.



- This data may not be given in size order
- The data forms information pairs for the scatter graph

Not all data has a relationship

The link between the data can be explained verbally

This scatter graph show as the age of a car increases the value decreases

8000-(Es)

The axis should fit all the values on and be equally spread out

Linear Correlation



Negative Correlation



Os one variable increases so does the other variable

Os one variable increases the other variable decreases

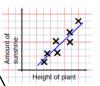
There is no relationship between the two variables

The line of best fit

The Line of best fit is used to make estimates about the information in your scatter graph

Things to know

- The line of best fit <u>DOES NOT</u> need to go through the origin (The point the axes cross)
- There should be approximately the same number of points above and below the line (It may not go through any points)
- The line extends across the whole



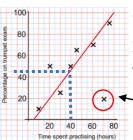
is only an estimate because the line is designed to be an average representation of the data

It is always a straight line.

Using a line of best fit

Interpolation is using the line of best fit to estimate values inside our data

e.g. 40 hours revising predicts a percentage of 45.



Extrapolation is where we use our line of best fit to predict information outside of our data

**This is not always useful — in this example you cannot score more that 100%. So revising for longer can not be estimated **

This point is an "outlier" It is an outlier because it doesn't fit this model and stands apart from

YFAR 10 - USING NUMBER

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Non-calculator methods

What do I need to be able to do?

Bu the end of this unit you should be able to:

- Use mental/written methods for the four number operations
- Use four operations for fractions
- Write exact answers
- Round to decimal places and significant figures
- Estimate solutions
- Understand limits of accuracy
- Understand financial maths

Keuwords

Truncate: to shorten, to shorten a number (no rounding), to shorten a shape (remove a part of the shape)

Round: making a number simpler, but keeping its place value close the what it originally was

Credit: money that goes into a bank account

Debit: money that leaves a bank account

Profit: the amount of money after income - costs

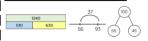
Tax: money that the government collects based on income, sales and other activities.

Balance: The amount of money in a bank account

Overestimate: Rounding up — gives a solution higher than the actual value

Underestimate: Rounding down — gives a solution lower than the actual value

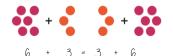
Oddition/Subtraction



Modelling methods for addition/subtraction

- Bar models
- Number lines
- Part/ Whole diagrams





The order of addition does not change the result

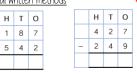
Subtraction the order has to stay the same



- Number lines help for addition and subtraction
- Working in 10's first aids mental addition/subtraction
- Show your relationships by writing fact families

Formal written methods

1



Remember the place value of each column. You may need to move 10 ones to the ones column to be able to subtract

Decimals have the same methods remember to align the place value

Division methods

Division with decimals

3584 ÷ 7 = 512

S<u>hort division</u> ³5

 $\div 24 = \div 6 \div 4$ Break up the divisor using

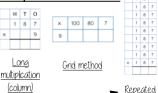
factors

The placeholder in division methods is essential — the decimal lines up on the dividend and the quotient

All give the same solution as represent the same proportion. Multiply the values in proportion until the divisor becomes an integer

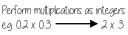
→ 24 ÷ 02 -

Multiplication methods



Less effective method especially for bigger multiplication

Multiplication with decimals



Make adjustments to your answer to match the question: $0.2 \times 10 = 2$ $0.3 \times 10 = 3$

Therefore 6 ÷ 100 = 0.06

Four operations with fractions

Od<u>dition and Subtraction</u>



Multiplication



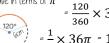
5

addition

Multiplying by a reciprocal gives the

outcome

Exact Values



 $=\frac{1}{2}\times 36\pi = 12\pi$



Tan 30 = $\frac{1}{\sqrt{3}}$

Estimation 🔃

Round to I significant figure to estimate

 $21.4 \times 3.1 \approx 20 \times 3 \approx 60$

The equal sign changes to show it is an estimation

This is an **underestimate** because both values were rounded down

It is good to check all calculations with an estimate in all aspects of maths — it helps you identify calculation errors.

Limits of accuracu

O width $oldsymbol{w}$ has been rounded to 6.4cm correct to ldp

< 6.35 the values > 6.45 the values wou Error interval would round to 6.3

The error interval

 $6.35 \le w < 6.45$

Only value within these limits would round to 6.4 to 1dp

O width \boldsymbol{w} has been truncated to 6.4cm correct to 1dp.

Error interval < 6.4 the values would truncate to 6.3 > 6.5 the values would

 $6.4 \le w < 6.5$

Ony value within these limits would truncate to 6.4 to 1dp

Rounding 🔃

2.46 192 (to 12dp) - Is this closer to 246 or 247



Significant Figures

247

This shows the number is closer

370 to 1 significant figure is 400 37 to 1 significant figure is 40 3.7 to I significant figure is 4

0.37 to I significant figure is 0.4 0.00000037 to 1 significant figure is 0.0000004 SF: Round to the first nonzero number

2.46 192

YEAR 10 - USING NUMBER..

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Types of number & sequences

What do I need to be able to do?

By the end of this unit you should be able to:

- Understand factors and multiples
- Express numbers as a product of primes
- Find the HCF and LCM
- Describe and continue sequences
- Explore sequences
- Find the nth term of a linear sequence

Keywords

Factor: numbers we multiply together to make another number

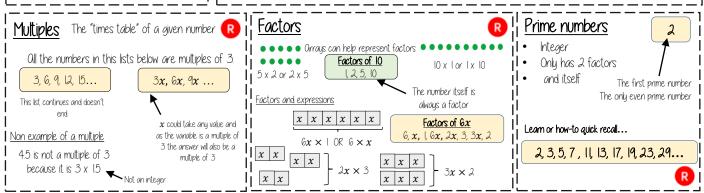
Multiple: the result of multiplying a number by an integer.

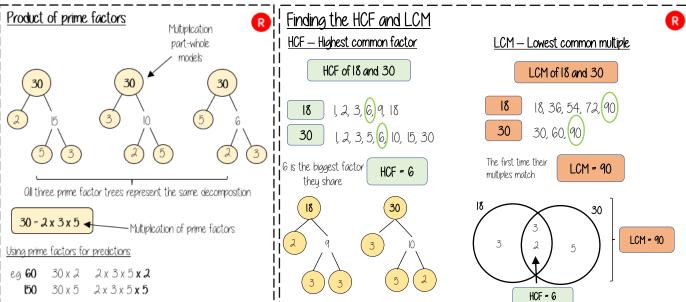
HCF: highest common factor. The biggest factor that numbers share.

LCM: lowest common multiple. The first multiple numbers share.

Orithmetic: a sequence where the difference between the terms is constant **Geometric**: a sequence where each term is found by multiplying the previous one by a fixed nonzero number

Sequence: items or numbers put in a pre-decided order





<u> Orithmetic/Geometric sequences</u>

Orithmetic Sequences change by a common difference. This is found by addition or subtraction between terms

Geometric Sequences change by a common ratio. This is found my multiplication/division between terms.

Term to term rule — how you get from one term (number in the sequence) to the next term.

Position to term rule — take the rule and substitute in a position to find a term Eg. Multiply the position number by 3 and then add 2.

11 Other sequences

Fibonacci Sequence 1, 1, 2, 3, 5, 8 ... Each term is the sum of the previous two terms

 $oxed{I}$ Triangular Numbers — look at the formation



II Square Numbers — look at the formation



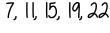
Sequences are the repetition of a patten

ii <u>Finding the nth term</u>

This is the 4 \longrightarrow 4, 8, 12, 16, 20....



This has the same constant difference — but is 3 more than the original sequence



4n+3

This is the constant difference between the terms in the sequence This is the comparison (difference) between the original and new sequence

YFAR 10 - USING NUMBER

144

Ony integer

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Indices & Roots

What do I need to be able to do?

By the end of this unit you should be able to:

- Identify square and cube numbers
- Calculate higher powers and roots
- Understand powers of 10 and standard
- Know the addition and subtraction rule for
- Understand power zero and negative indices
- Calculate with numbers in standard form

Keywords

Standard (index) Form: A system of writing very big or very small numbers

Commutative: an operation is commutative if changing the order does not change the result.

Base: The number that gets multiplied by a power

Power: The exponent — or the number that tells you how many times to use the number in multiplication. Exponent: The power — or the number that tells you how many times to use the number in multiplication.

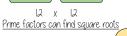
Indices: The power or the exponent.

Negative: a value below zero...

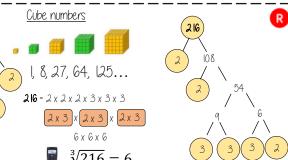
Coefficient: The number used to multiply a variable

Square and cube numbers Square numbers









100

10-2

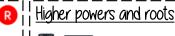
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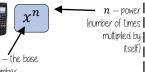
10-3

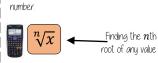
Negative powers do not

indicate negative solutions









Other mental strategies for square roots

$\sqrt{810000} = \sqrt{81} \times \sqrt{10000}$ $= 9 \times 100$

= 900

Standard form





Example Non-example

3.2 x 10 4 = 3.2 x 10 x 10 x 10 x 10

= 32000

0.8 x 10 4

5.3 x 10⁰⁷

Numbers in standard form with negative

0.001

 $|\chi|_{\frac{1}{1000}}$

1 x 10-3

powers will be less than I

Ony value to the power O always = 1

 $3.2 \times 10^{-4} = 3.2 \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} \times \frac{1}{10} = 000032$

Oddition/Subtraction Laws

 $a^m \times a^n = a^{m+n}$

 $a^m \div a^n = a^{m-n}$

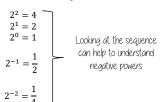
Zero and negative indices

$$x^0 = 1$$

$$\frac{a^6}{a^6} = a^6 \div a^6$$

$$= a^{6-6} = a^0 = 1$$

Negative indices do not indicate negative solutions



Powers of powers

$$(x^a)^b = x^{ab}$$

$$(2^3)^4 = 2^3 \times 2^3 \times 2^3 \times 2^3$$

The same base and power is repeated Use the addition

$$(2^3)^4 = 2^{12} - a \times b = 3 \times 4 = 12$$

NOTICE the difference

$$(2x^3)^4 = 2x^3 \times 2x^3 \times 2x^3 \times 2x^3$$

The addition law applies ONLY to the powers. The integers still need to be multiplied

The integers still need to be multiplied
$$(2x^3)^4=16x^{12}$$

Standard form calculations



Tip: Convert into ordinary numbers first and back to standard from at

$6 \times 10^5 + 8 \times 10^5$ Method I

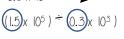
- = 600000 + 800000
- = 1400000
- $= 1.4 \times 10^{5}$
- final answer
- This is not the
- 14 x 10⁵ 1.4 x 101 x 105 = 1.4 x 10⁵

Method 2

 $= (6 + 8) \times 10^{5}$

Multiplication and division

Division questions can look like this 0.3×10^{3}





 $=5 \times 10^{2}$

For multiplication and division you can look at the values for A and the powers of 10 as two separate calculations