# YEAR 10 - SIMILARITY... @whisto_maths Congruence, similarity $\varepsilon$ enlargement 

## What do I need to be able to do?

By the end of this unit you should be able
to:

- Enlarge by a positive scale factor
- Enlarge by a fractional scale factor
- Identify similar shapes
- Work out missing sides and angles in similar shapes
- Use parallel lines to find missing angles
- Understand similarity and congruence


## Keywords

Enlarge: to make a shape bigger (or smaller) by a given mutipilier (scale factor)
Scale Factor: the mutipitier of enlargement
Centre of enlargement: the point the shape is enlarged from
Simiar: when one shape can become another with a reflection, rotation, enlargement or translation.
Congruent: the same size and shape
Corresponding: tems that appear in the same place in two similar situations
Paralle: straight lines that never meet (equal gradients)

Positive scale factors $R$
Enlargement from a point
Enlarge shape $A$ by SF 2 from $(0,0)$

The shape is enlarged by 2

The distance from the point enlarges by 2


1) Identify similar shapes


Information in similar shapes



Co-interior angles


As angles on a line add up to $180^{\circ}$ co-interior angles can also be calculated from applying alternate/ corresponding rules first

## Similar triangles



1

## Conavence and Similarity

Congruent shapes are identical - all corresponding sides and angles are the same size


Because al angles are the same, but all sides are enlarged by 2 OBC and HU are similar

I Conditions for congruent triangles
| | Triangles are congruent if they satisfy any of the following conditions
1
I I Ill three sides on the triangle are the same size

## angle-side-angle

Two angles and the side connecting them are equal in two triangles

Side-angle-side
Two sides and the angle in-between them are equal in two
I triangles (it will also mean the third side is the same size on
I both shapes)
Right angle-hypotenuse-side
I The triangles both have a right angle, the hypotenuse and I one side are the same

## YeAR 10 －SIMLARITY．．．

## ＠whisto＿maths

## Trigonometry


$a: b$
$x: 100$

$a: b$ 0.07 ：$x$ $0.07: 0.14$

When the angle is the same the ratio of sides $a$ and $b$ will also remain the same II

## Keywords

II Enlarge：to make a shape bigger（or smaller）by a given mutipilier（scale factor）
II Scale Factor：the mutipier of enlargement
II Constant：a value that remains the same
II Cosine ratio：the ratio of the length of the adjacent side to that of the hypotenuse．The sine of the complement．
I｜Sine ratio：the ratio of the length of the opposite side to that of the hypotenuse．
II Tangent ratio：the ratio of the length of the opposite side to that of the adjacent side．
II Inverse：function that has the opposite effect．
II Hypotenuse：longest side of a right－angled triangle．It is the side opposite the right－angle

Hypotenuse，adjacent and opposite ONLY right－angled trangles are abeled in OPPOSITE
II always opposite an acute angle
II Useful to label second
II Position depend upon the angle
II
in use for the question

## Tangent ratio：side lengths

$\operatorname{Tan} \theta=\frac{\text { opposite side }}{\text { adjacent side }}$

Sin，Cos，Tan：Angles
Inverse trigonometric functions


Sin and Cos ratio：side lengths

## yEAR 10 －DEVELOPING ALGEBRA． Representing solutions of equations and ＠uhisto＿maths <br> What do I need to be able to do？ <br> By the end of this unit you should be able to： <br> －Form and solve equations and inequalities <br> －Represent and interpret solutions on a number line as inequalities <br> Draw straight line graphs and find solutions to equations <br> Form and solve equations and inequalities with unknowns on both sides <br> Keymords <br> Solution：a value we can put in place of a variable that makes the equation true <br> Variable：a symbol for a number we don＇t know yet． <br> Equation：an equation says that two things are equal－it will have an equals sign $=$ <br> Expression：numbers，symbols and operators grouped together to show the value of something <br> Identity：An equation where both sides have variables that cause the same answer includes $\equiv$ Linear：an equation or function that is the equation of a straight line <br> Intersection：the point that two lines meet <br> Inequality：an inequality compares two values showing if one is greater than，less than or equal to <br> another．

Form and solve inequalties $R$
$3(2 x+4)=30$

Expand the brackets
$6 x+12=30$
$6 x=18$


Solve
$x \longleftarrow-3 \longleftarrow-2 \longleftarrow<$
 $x>3$

Solutions on a number line


Includes the value

includes the value I

Values less than or equal to 3 but also more than－I


This includes the integer values $0,1,2,3$

Pbtting straight ine araphs $\mathbb{B}$


Equations：unknown on both sides $R$
$8 x+5=4 x+13$

$8 x+5=4 x+13$
$-4 x \quad-4 x$
$4 x+5=13$
$-5 \quad-5$
$\div 4 \begin{gathered}4 x=8 \\ x=2\end{gathered} \div 4$
ーニニニニニニニニニニニニニニニニニニニー 7
Inequalities：unknown on both sides

$$
8 x+5 \leq 4 x+13] \longrightarrow x \leq 2
$$

any value 2 or less will satisfy this inequality

## YEAR 10 - DEVELOPING ALGEBRA. <br> @uhisto_maths

What do I need to be able to do?
By the end of this unit you should be able to:

- Determine whether $(x y)$ is a solition
- Solve by substituting a known variable
- Solve by substituting an expression
| - Solve graphically
I - Solve by subtracting adding equations
- Solve by adjusting equations
- Form and solve linear simutaneous


## Keywords

Solution: a value we can put in place of a variable that makes the equation true
I V Variable: a symbol for a number we don't know yet.
I Equation: an equation says that two things are equal - it will have an equals sian $=$
I Substitute: replace a variable with a numerical value
I LCM: lowest common mutiple (the first time the times table of two or more numbers match)
1 Eliminate: to remove
Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign) Coordinate: a set of values that show an exact position
I Intersection: the point two lines cross or meet.

Is $(x, y)$ a solution? $\times$ and $y$ represent values
that can be substituted into that can be substituted into an equation


Substituting known varababes.
Stephanie knows the point $x=4$ les on that line. Find the value for $y$.
a line has the equation $3 x+y=14$
$3 x+y=14$

$3(4)+y=14$

Two different variables, two solutions
$12+y=14$
$x=4$

$$
y=2
$$

ISOlve by subtraction
Solve craphicialy


$x=4$
$y=3$
addition makes zero pairs II Solve by adjusting one


Solve by addition

| $3 x+2 y$ | $=16$ |
| ---: | :--- |
| $+6 x-2 y$ | $=2$ |
| $9 x$ | $=18$ |
| $\div 9$ | $\div 9$ |

$$
3 x+2 y=16
$$

$$
3(2)+2(y)=16
$$

$$
6+2 y=16
$$

$$
-6 \quad-6
$$

$$
2 y=10
$$

$$
y=5
$$

By proportionally adjusting one of
29

| Solve by adjusting one | 12 |
| :---: | :---: |
|  | $\stackrel{\square}{\square}$ |
|  | $n$  |
|  | $n$ $n$ 1 1 $j$ |
| $2 h+2 j=29$ | $\xrightarrow{ }$ |
|  | 29 |
|  | 24 |
| $2 h+2 j=24$ | $\stackrel{\square}{\square+1}$ |
| $2 h+2 j=29$ | $n$ $n$ $i$ $i$ <br> $n$    |
| $2 h+2 j=29$ | $n$ $n$ $i$ $j$ $i$ |
|  | $\xrightarrow[29]{ }$ |
| By proportionally adjusting one of | 29 |
| the equations - now solve the |  |
| simuttaneous equations choosing |  |
| an addition or subtraction method |  |

Solve by adjusting both
$2 x+3 y=39$
$5 x-2 y=-7$


Use LCM to make equivalent x OR y values Because of the negative values using zero pairs and $y$ values is chosen choice

$y=5$

