YEAR 10 - SIMILARITY

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Congruence, similarity & enlargement

What do I need to be able to do?

By the end of this unit you should be able

- Enlarge by a positive scale factor
- Enlarge by a fractional scale factor
- Identify similar shapes
- Work out missing sides and angles in similar shapes
- Use parallel lines to find missing angles
- Understand similarity and congruence

Keywords

Enlarge: to make a shape bigger (or smaller) by a given multiplier (scale factor)

Scale Factor: the multiplier of enlargement

Centre of enlargement: the point the shape is enlarged from

Similar: when one shape can become another with a reflection, rotation, enlargement or translation.

Conaruent: the same size and shape

Corresponding: items that appear in the same place in two similar situations

Parallel: straight lines that never meet (equal gradients)

Positive scale factors 🕟

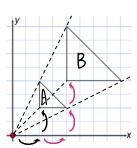


Enlargement from a point

Enlarge shape A by SF 2 from (0,0)

The shape is enlarged by 2

The distance from the point enlarges by 2

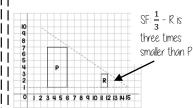


Fractional scale factors



Fractions less than I make a shape SMOLLER

R is an enlargement of P by a scale factor $\frac{1}{2}$ from centre of enlargement (15,1)



Identify similar shapes



Ongles in similar shapes do not

e.g. if a triangle gets bigger the angles can not go above 1800





Scale Factor: Both sides on the bigger

Because co-interior angles have

shape are 15 times bigger

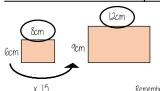
Compare

8:12

Both sets of sides are in the same ratio

Co-interior angles

Information in similar shapes



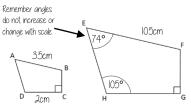
Scale Factor is the multiplicative relationship between the two **kngths**

Shape OBCD and EFGH are similar

Notation helps us corresponding sides

OB and EF are corresponding

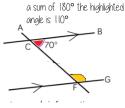
Olternate angles Compare the equivalent side on both shapes



Ongles in parallel lines



Because alternate angles are equal the highlighted angles are the same size

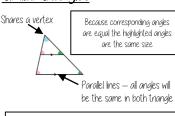


Corresponding angles

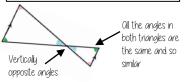
Because corresponding angles are equal the highlighted angles are the same size

Os angles on a line add up to 180° co-interior angles can also be calculated from applying alternate/corresponding rules

Similar triangles

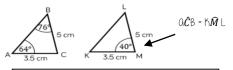


Os all angles are the same this is similar — it only one pair of sides are needed to show equality

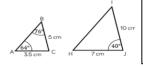


Congruence and Similarity

Congruent shapes are identical — all corresponding sides and angles are the same size



Because all the angles are the same and OC=KM BC=LM triangles OBC and KLM are congruent



Because all angles are the same, but all sides are enlarged by 2 OBC and HLJ are

i Conditions for congruent triangles

Triangles are congruent if they satisfy any of the following conditions

Side-side-side

| All three sides on the triangle are the same size

Ongle-side-angle

Two angles and the side connecting them are equal in two triangles

Side-angle-side

Two sides and the angle in-between them are equal in two I triangles (it will also mean the third side is the same size on ! I both shapes)

Right angle-hypotenuse-side

The triangles both have a right angle, the hypotenuse and I one side are the same

YFAR 10 - SIMILARITY...

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Trigonometry

What do I need to be able to do?

By the end of this unit you should be able to:

- Work fluently with hypotenuse, opposite and adjacent sides
- Use the tan, sine and cosine ratio to find missing side lengths
- Use the tan, sine and cosine ratio to find missing anales
- Calculate sides using Pythagoras'

Keywords

When the angle is the same

Enlarge: to make a shape bigger (or smaller) by a given multiplier (scale factor)

Scale Factor: the multiplier of enlargement

Constant: a value that remains the same

Cosine ratio: the ratio of the length of the adjacent side to that of the hypotenuse. The sine of the complement

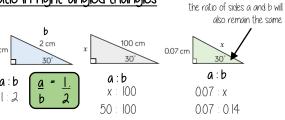
Sine ratio: the ratio of the length of the opposite side to that of the hypotenuse.

Tangent ratio: the ratio of the length of the opposite side to that of the adjacent side.

Inverse: function that has the opposite effect.

Hypoteruse: longest side of a right-angled triangle. It is the side opposite the right-angle

Ratio in right-angled triangles

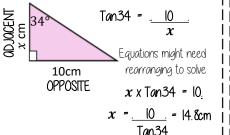


Hupotenuse, adjacent and opposite ONLY right-angled triangles are labelled in **ADJACENT** OPPOSITE Next to the angle in question Often labelled last Olways opposite an acute angle Useful to label second Position depend upon the angle Olways the longest side in use for the question HYPOTENUSE always opposite the right angle

Tangent ratio: side lengths

 $Tan\theta$ = opposite side adjacent side

Substitute the values into the tangent formula !



Sin and Cos ratio: side lengths

OPPOSITE $Sin\theta$ = opposite side x cmhupotenuse side NOTE The Sin(x) ratio is 12 cm HYPOTENUSE the same as the Cos(90-x) ratio

 $Cos\theta$ = adjacent side **ADJACENT** hypotenuse side x cm40° Substitute the values into the

12 cm

Useful to label this first

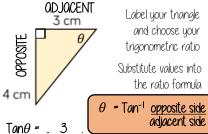
ratio formula HYPOTENUSE

Equations might need rearranging to solve

Sin, Cos, Tan: Ongles

 $\theta = 36.9^{\circ}$

Inverse trigonometric functions



 θ = Sin⁻¹ opposite side hypotenuse side θ = Tan⁻¹ 3

> = Cos-1 adiacent side hypotenuse side

Pythagoras theorem 🔞 Hupotenuse² = $a^2 + b^2$

This is commutative — the square of the hypotenuse is equal to the sum of the squares of the two shorter

Cos45 =

Places to look out for Pythagoras Perpendicular heights in isosceles

- trianales
- Diagonals on right angled shapes
- Distance between coordinates
- Ony length made from a right angles

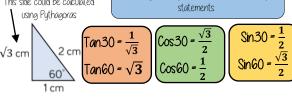
Key anales 0° and 90°

Keu anales

1 cm

1 cm

Because trig ratios remain the same for similar shapes you can generalise from the following This side could be calculated statements. using Pythagoras



Tan45 = 1

This value cannot be defined — it is impossible as you cannot have two 90° angles in a triangle

Tan0 = 0

Sin0 = 0

Sin45 =

Sin90 = 1

Cos0 = 1Cos90 = 0

YEAR 10 — DEVELOPING ALGEBRA

Representing solutions of equations and

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inequalities

What do I need to be able to do?

By the end of this unit you should be able

- Form and solve equations and inequalities
- Represent and interpret solutions on a number line as inequalities
- Draw straight line graphs and find solutions to equations
- Form and solve equations and inequalities with unknowns on both sides

Keywords

Solution: a value we can put in place of a variable that makes the equation true

Variable: a sumbol for a number we don't know yet

Equation: an equation says that two things are equal - it will have an equals sign =

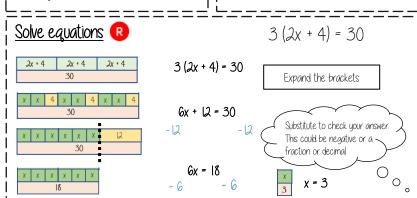
Expression: numbers, symbols and operators grouped together to show the value of something

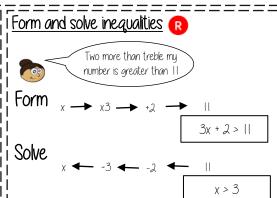
Identitu: On equation where both sides have variables that cause the same answer includes \equiv

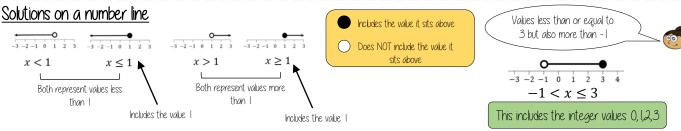
Linear: an equation or function that is the equation of a straight line

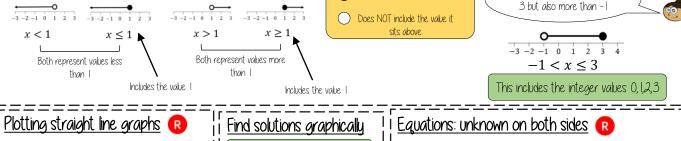
Intersection: the point that two lines meet

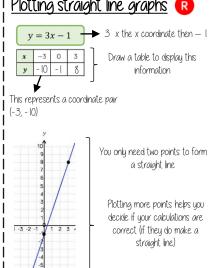
Inequality: an inequality compares two values showing if one is greater than, less than or equal to another.



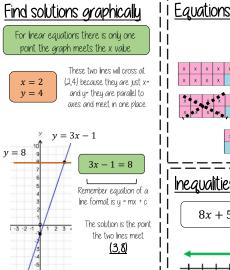


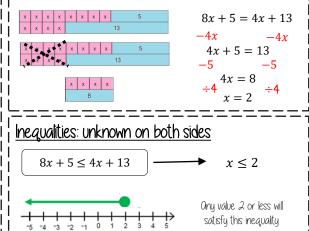






Remember to join the points to make a line





8x + 5 = 4x + 13

YEAR 10 - DEVELOPING ALGEBRA...

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Simultaneous Equations

x = 2y

What do I need to be able to do?

By the end of this unit you should be able to:

- Determine whether (x,y) is a solution
- Solve by substituting a known variable
- Solve by substituting an expression.
- Solve graphically
- Solve by subtracting/ adding equations
- Solve by adjusting equations
- Form and solve linear simultaneous equations

Keywords

Solution: a value we can put in place of a variable that makes the equation true

Variable: a symbol for a number we don't know yet.

Equation: an equation says that two things are equal - it will have an equal sign = 1

Substitute: replace a variable with a numerical value

LCM: lowest common multiple (the first time the times table of two or more numbers match)

Eliminate: to remove

Expression: a maths sentence with a minimum of two numbers and at least one math operation (no equals sign)

Coordinate: a set of values that show an exact position.

Intersection: the point two lines cross or meet

